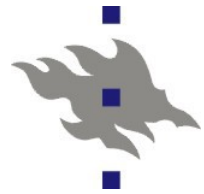


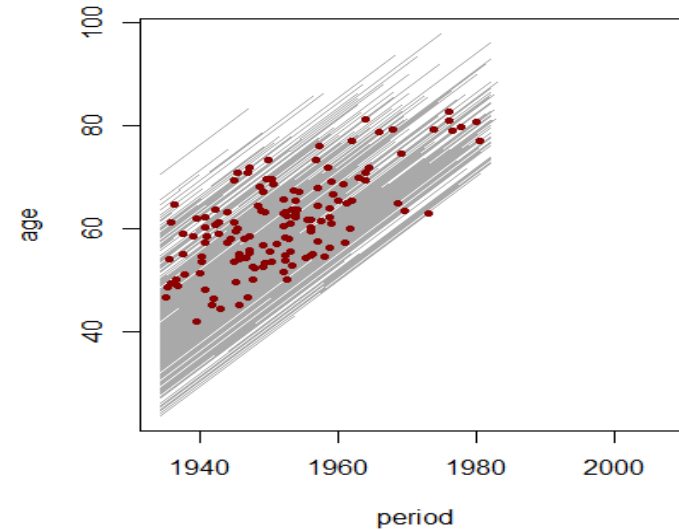
# Methodological challenges in research on consequences of sickness absence and disability pension?

Prof. Jari Haukka, PhD  
Hjelt Institute, University of Helsinki

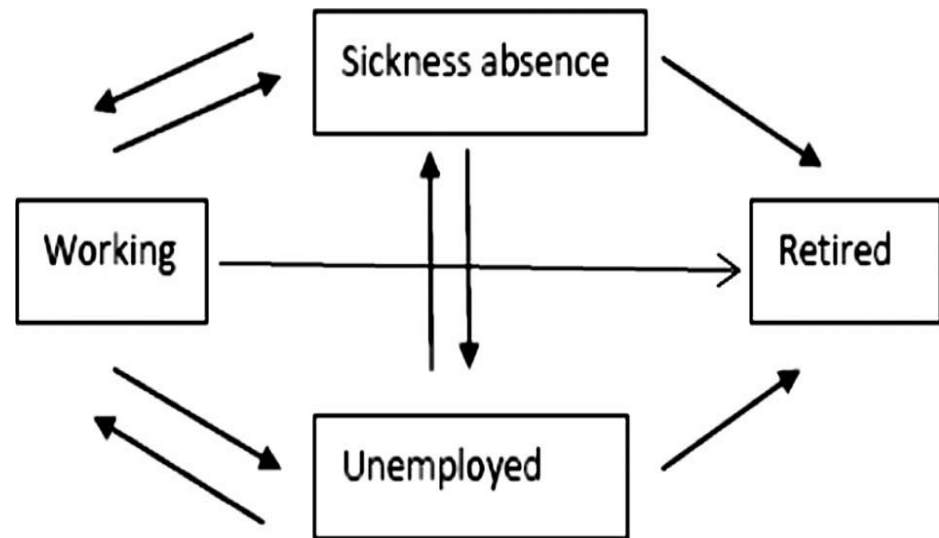


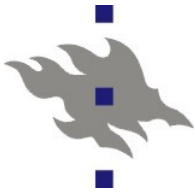
# Two methodological approaches

Lexis diagrams and  
Poisson regression



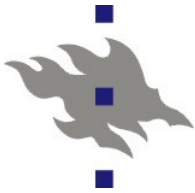
Multi state modeling





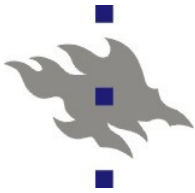
# Poisson regression

- The Cox proportional hazards model use only one time scale
- Alternative is to use Poisson regression with a piecewise-constant hazard
- Typically 5-years timebands of age and calendar year are used.



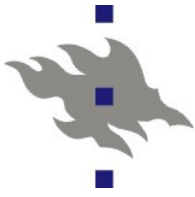
# Poisson regression

- Quite sophisticated analysis could be carried out by Poisson regression
- Follow-up time could be split by event in interest e.g.:
  - E.g. by first prescription of certain drug
  - first long sickness leave
  - first hospitalization
- Times could be modeled using splines that provides good tools for data-analysis



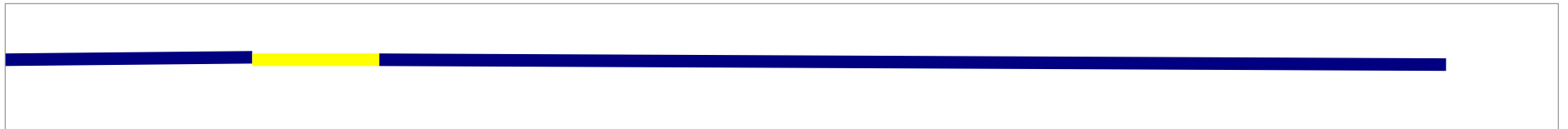
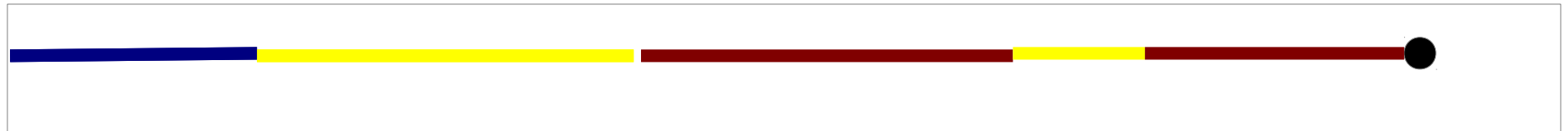
# Sick-leave data time scales





- Time since start of follow-up
- Time since start of antidepressants
- Time since cessation of antidepressants
- Time since cessation of last sick-leave
- Age
- Calendar time



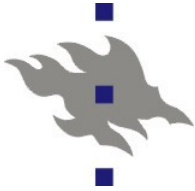
# Lexis and multiple time scales

## Two sample individuals

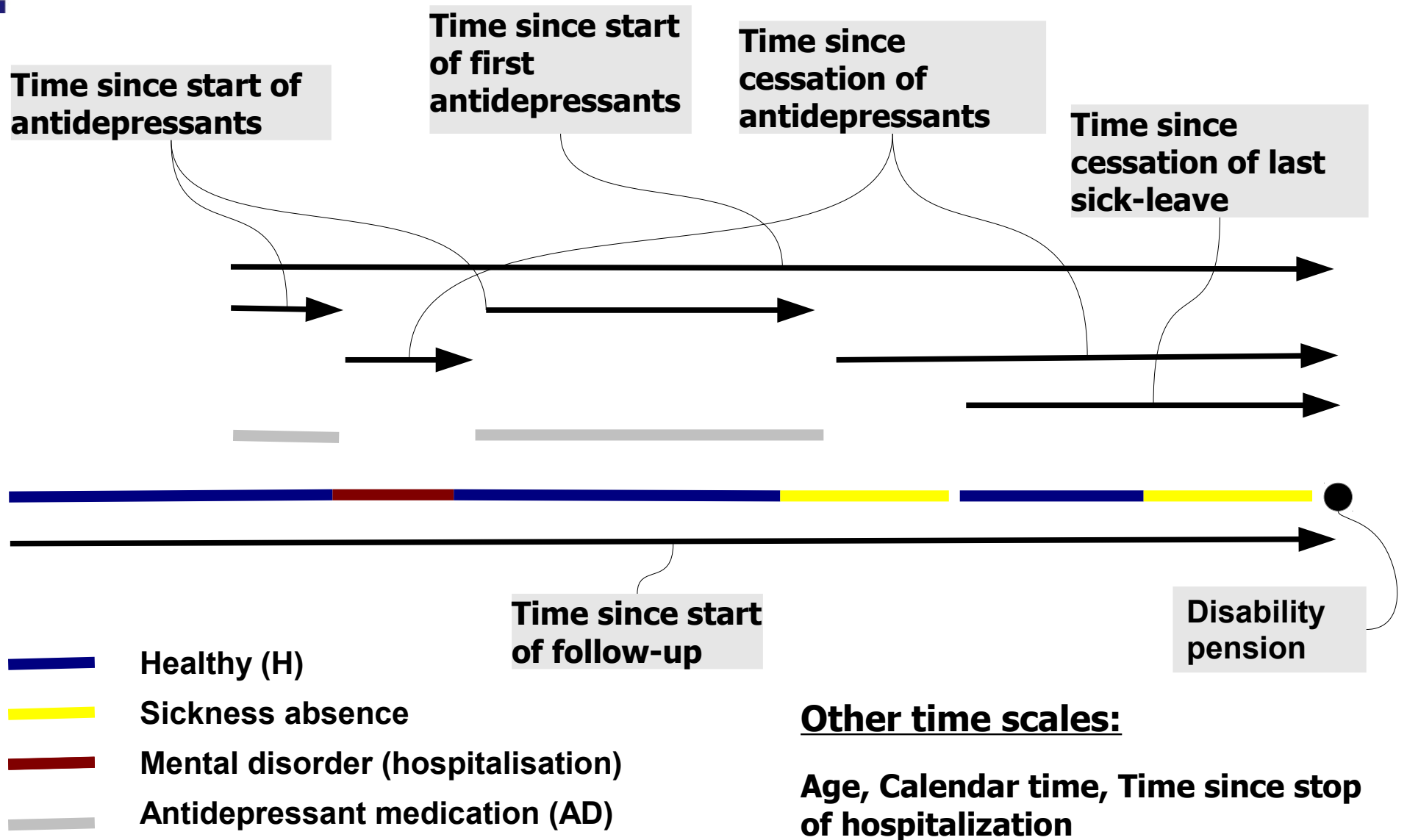


-  Healthy (H)
-  Sickness absence
-  Mental disorder (after first hospitalisation)
-  Death

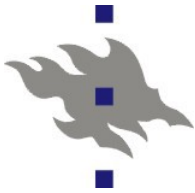
Time since  
start of follow-up



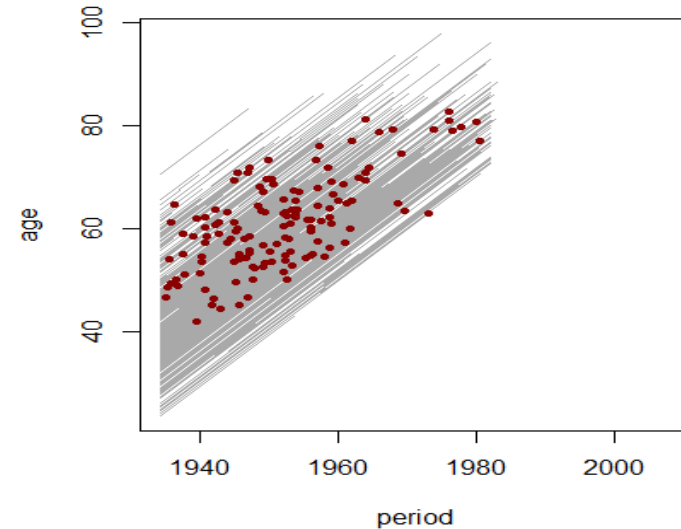
# Time-scales



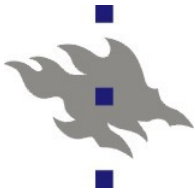




# Lexis diagrams



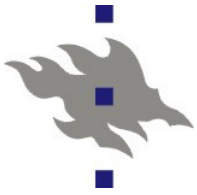
- Examples from :
  - Carstensen B, Plummer M. Using Lexis Objects for Multi-State Models in R. *Journal of Statistical Software* 2011;38:1–18.
  - Carstensen B. Age–period–cohort models for the Lexis diagram. *Statistics in Medicine* 2007;26:3018–45.
  - Plummer M, Carstensen B. Lexis: An R Class for Epidemiological Studies with Long-Term Follow-Up. *Journal of Statistical Software* 2011;38:1–12.
- **Example data:** The data concern a cohort of nickel smelting workers in South Wales and are taken from Breslow and Day, Volume 2. For comparison purposes, England and Wales mortality rates (per 1,000,000 per annum) from lung cancer (ICDs 162 and 163), nasal cancer (ICD 160), and all causes, by age group and calendar period, are supplied in the dataset ewrates.



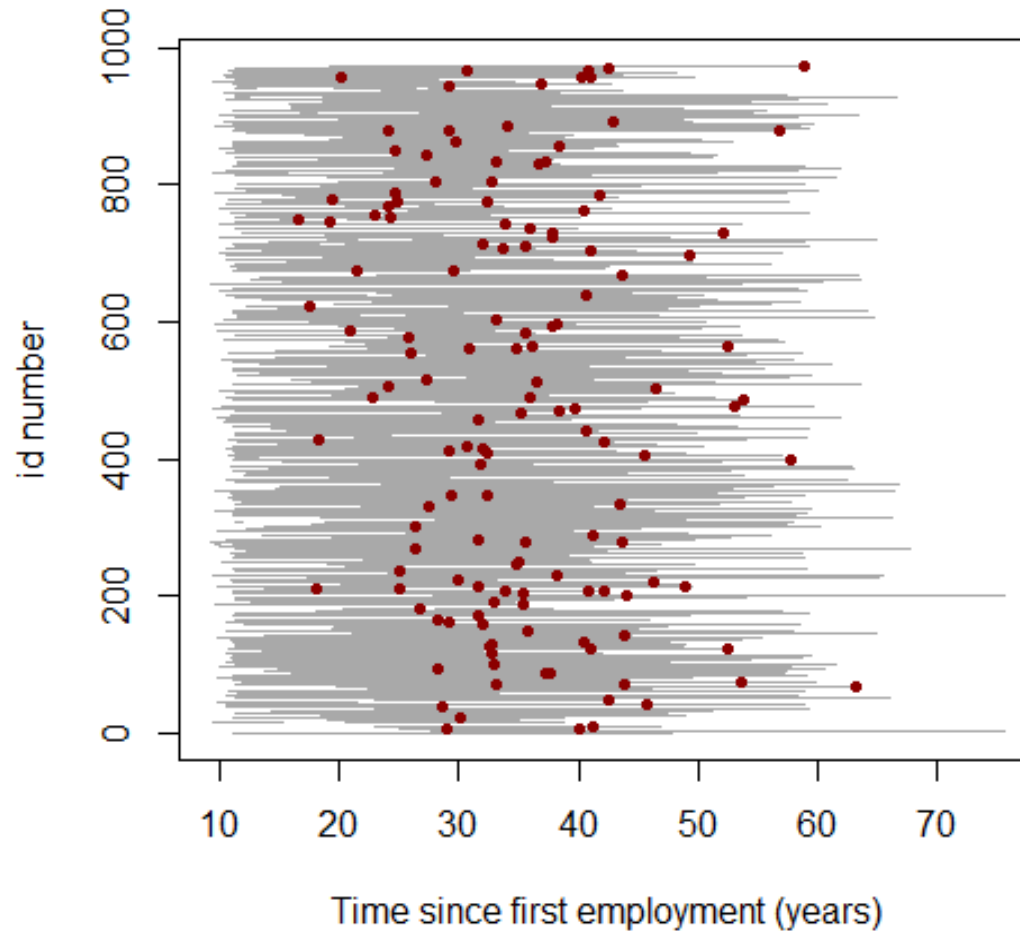
# Nickel data

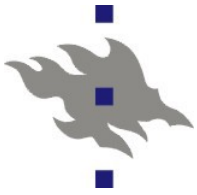
- Example data

```
> head(nickel)
  id icd exposure      dob  age1st  agein  ageout
1  3   0         5 1889.019 17.4808 45.2273 92.9808
2  4 162         5 1885.978 23.1864 48.2684 63.2712
3  6 163        10 1881.255 25.2452 52.9917 54.1644
4  8 527         9 1886.340 24.7206 47.9067 69.6794
5  9 150         0 1879.500 29.9575 54.7465 76.8442
6 10 163         2 1889.915 21.2877 44.3314 62.5413
>
```

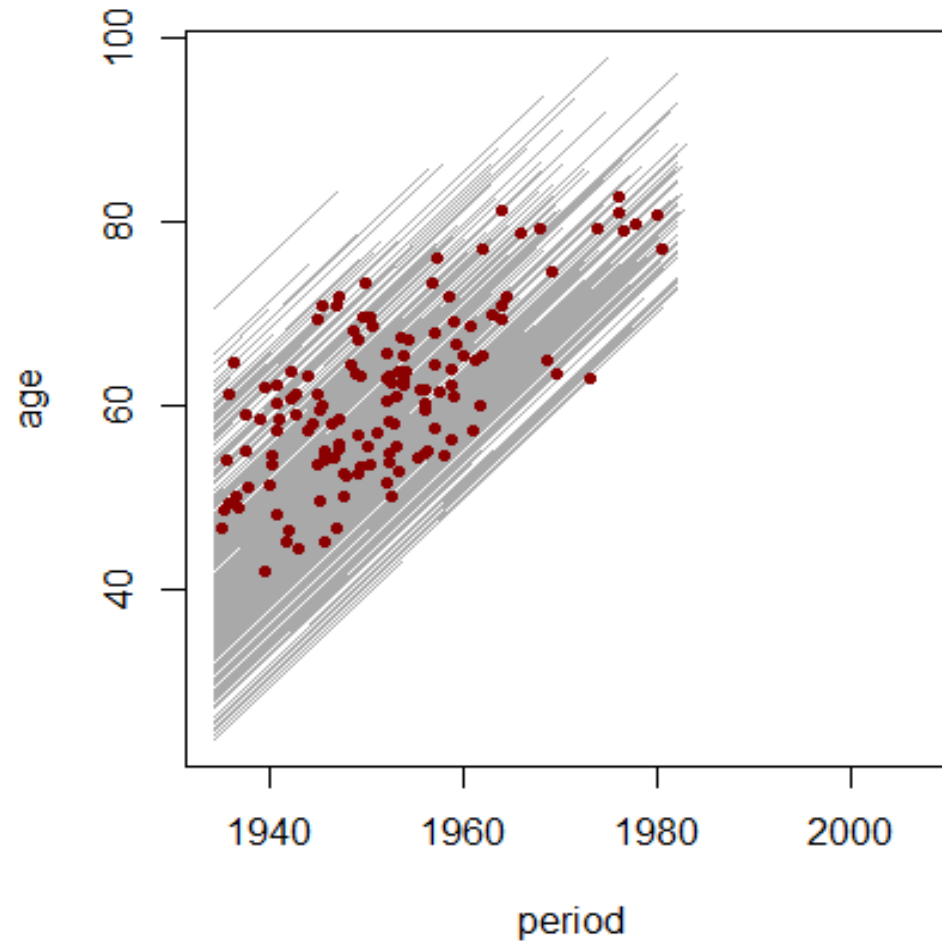


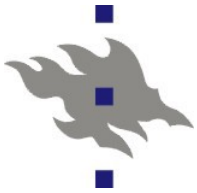
# Lexis, one time scale



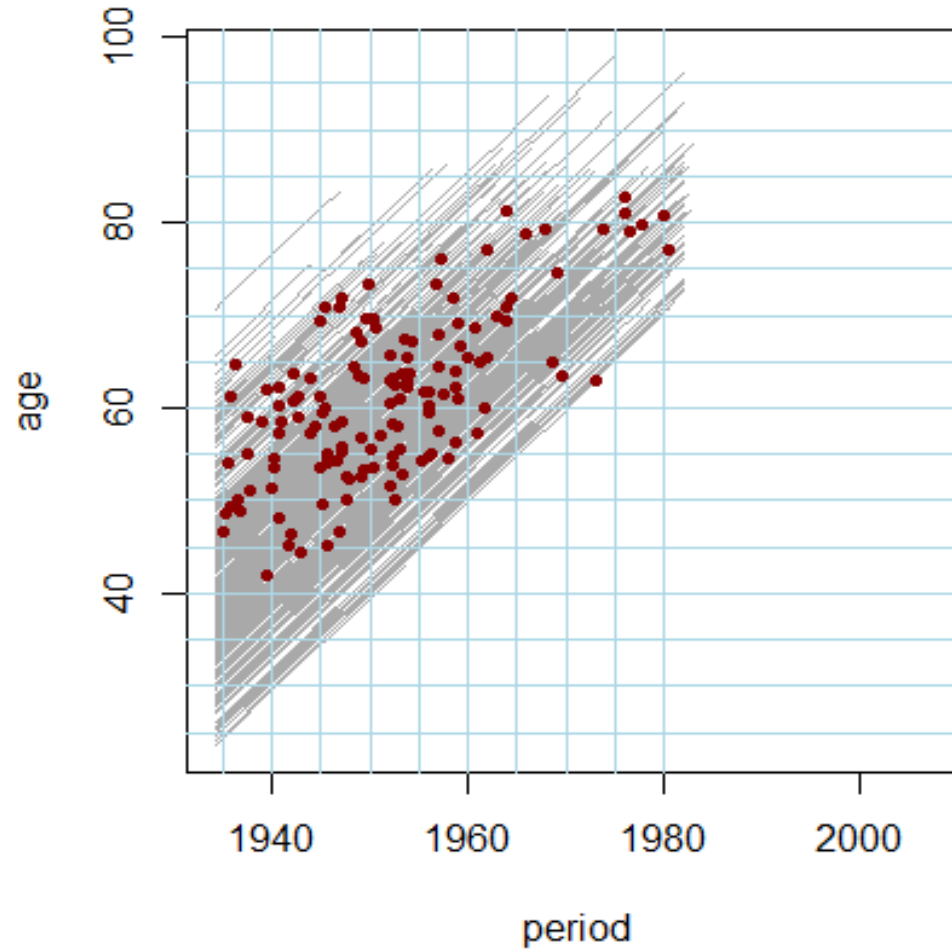


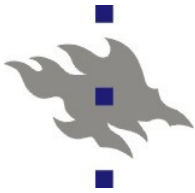
# Lexis, two time scales





# Lexis, two time scales, 5 yrs



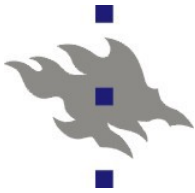


# Modeling data (1)

- Variables for three time scale, viz. period, age and time since first exposure

```
> subset(nicS2, id==4, select = c("case", "period", "age",  
"tfe", "lex.dur"))
```

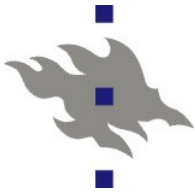
	case	period	age	tfe	lex.dur
7	FALSE	1934.246	48.2684	25.0820	1.7316
8	FALSE	1935.978	50.0000	26.8136	3.1864
9	FALSE	1939.164	53.1864	30.0000	6.8136
10	TRUE	1945.978	60.0000	36.8136	3.2712



# Modeling data (2)

```
library( Hmisc )
library( rms )
library(Epi)
# Model with age and time since first exposure
# NOTE!
# function "rcs" applies restricted cubic spline with
# user specified knots

tmp.m1.2<-glm(case ~
  rcs(age,parms=c(30,50,70)) +
  rcs(tfe,parms=c(10,20,30,40)) +
  offset(log(pyar)),
  family = poisson(),
  subset = (age >= 40), data = nicS2)
```



# Modeling data (3)

```
> (tmp.m1.2)
```

```
Call: glm(formula = case ~ rcs(age, parms = c(30, 50, 70)) + rcs(tfe,  
      parms = c(10, 20, 30, 40)) + offset(log(pyar)), family = poisson(),  
      data = nicS2, subset = (age >= 40))
```

Coefficients:

```
              (Intercept)  
              -13.23426  
  rcs(age, parms = c(30, 50, 70))age  
              0.13467  
  rcs(age, parms = c(30, 50, 70))age'  
              -0.09365  
  rcs(tfe, parms = c(10, 20, 30, 40))tfe  
              0.11148  
  rcs(tfe, parms = c(10, 20, 30, 40))tfe'  
              -0.10678  
  rcs(tfe, parms = c(10, 20, 30, 40))tfe''  
              0.08234
```

```
Degrees of Freedom: 2757 Total (i.e. Null); 2752 Residual
```

```
Null Deviance: 999.4
```

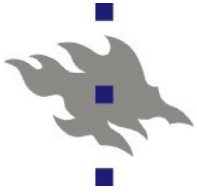
```
Residual Deviance: 968.7 AIC: 1255
```

**Interpretation of  
spline parameters is  
difficult.**

**->**

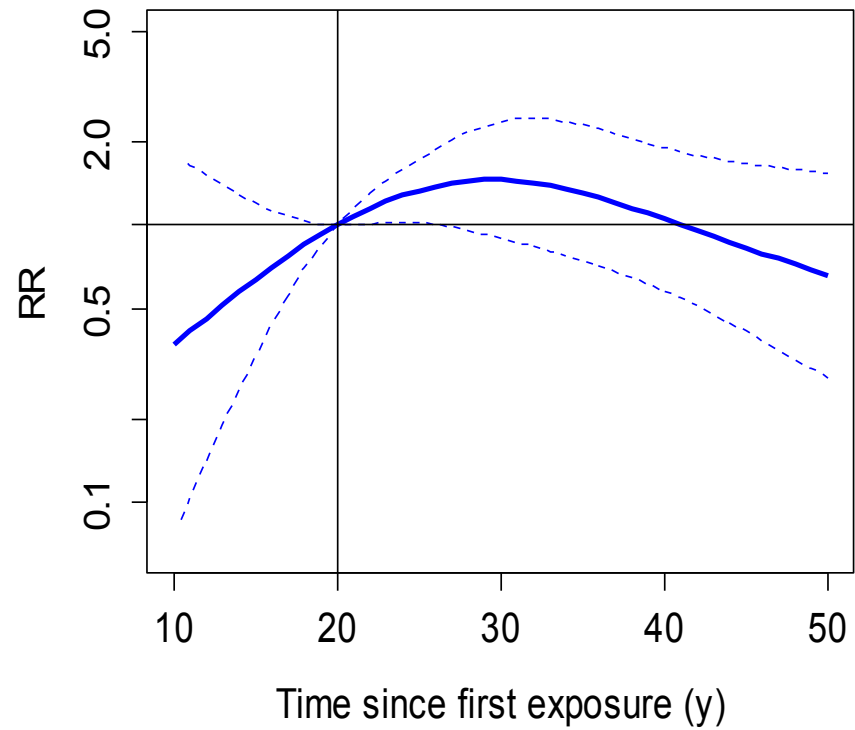
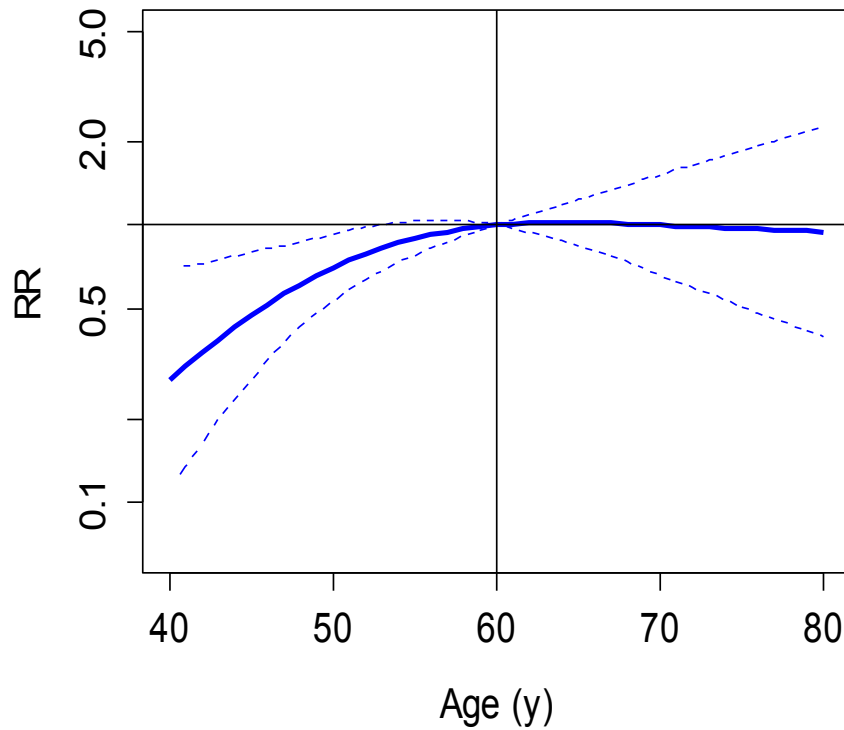
**Present results as  
graphs**

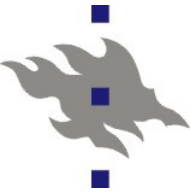




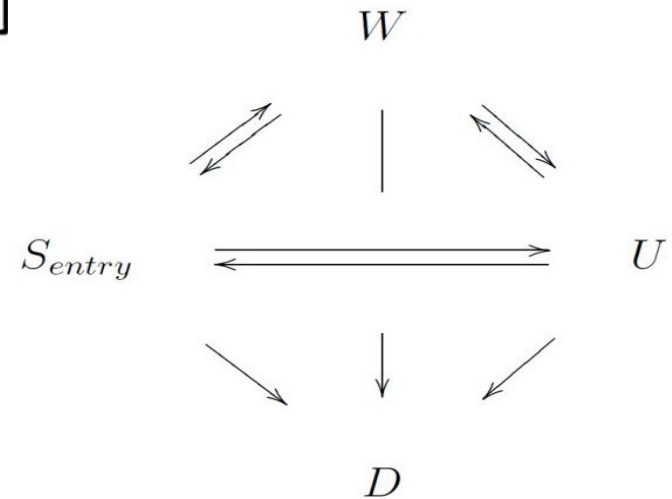
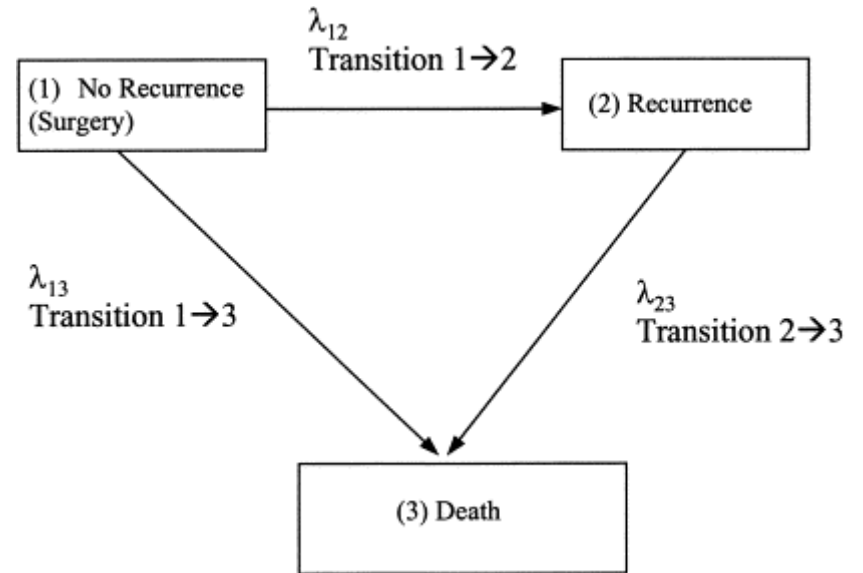
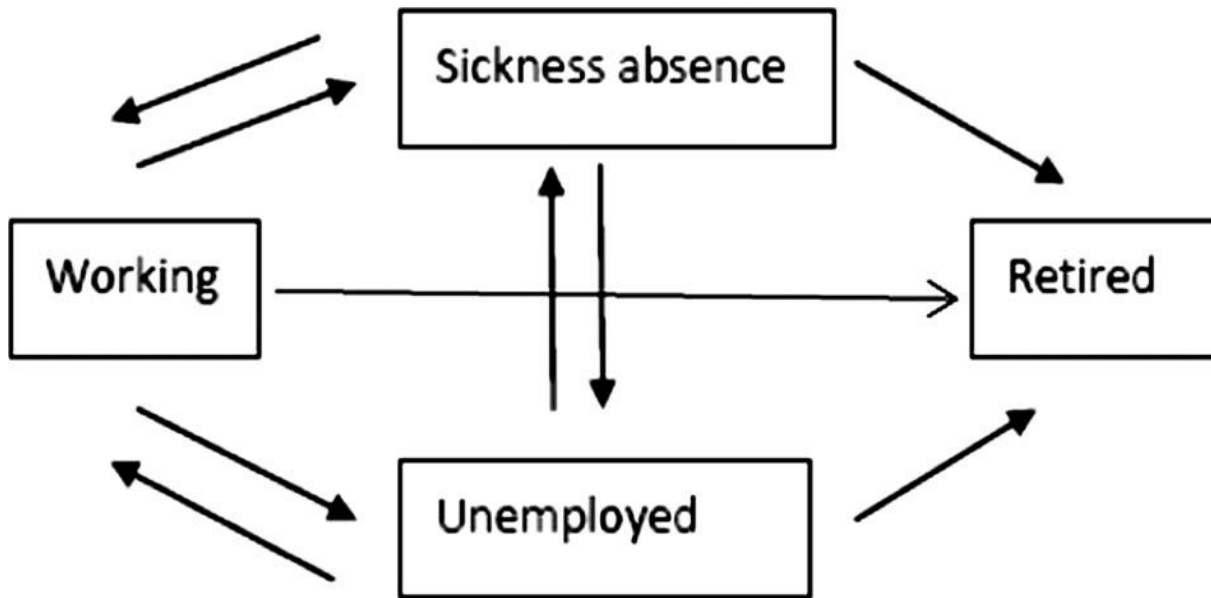
# Modeling data (4)

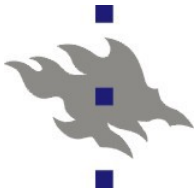
Rate ratios (RR) with 95% CI presented in graphics.





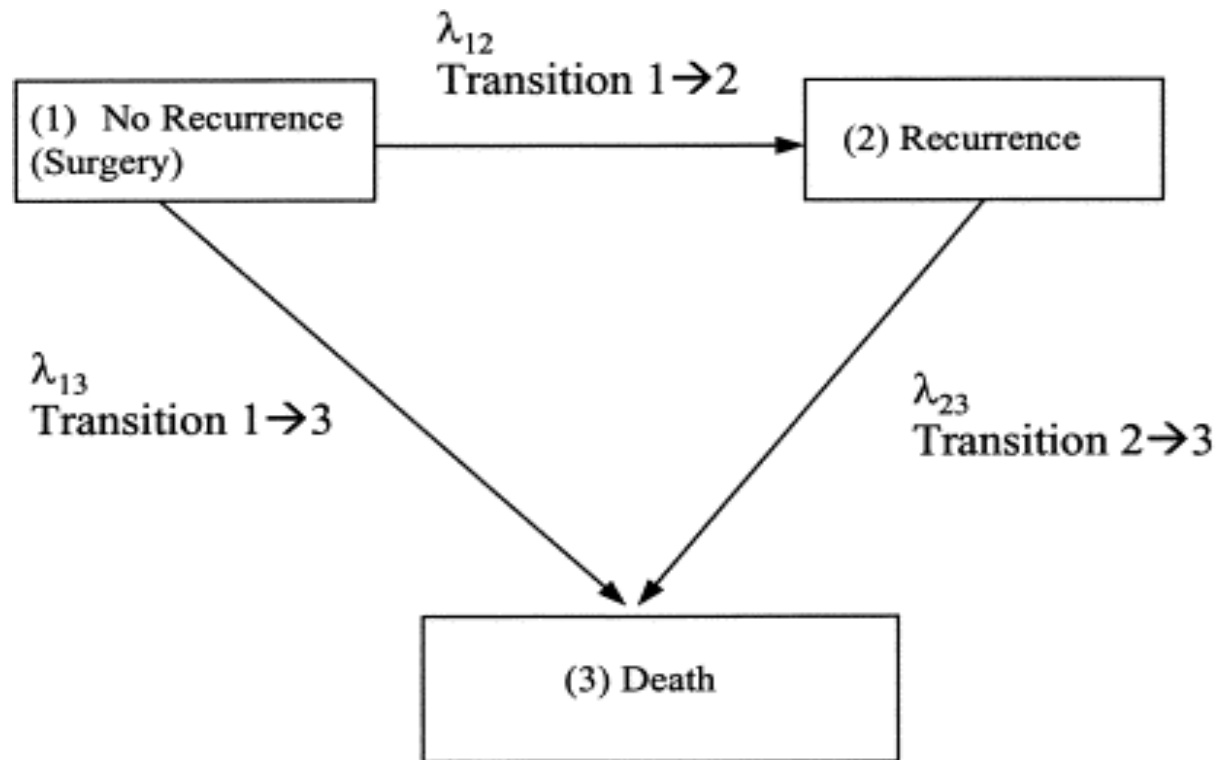
# Multi state modeling

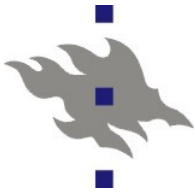




# Multi state modeling

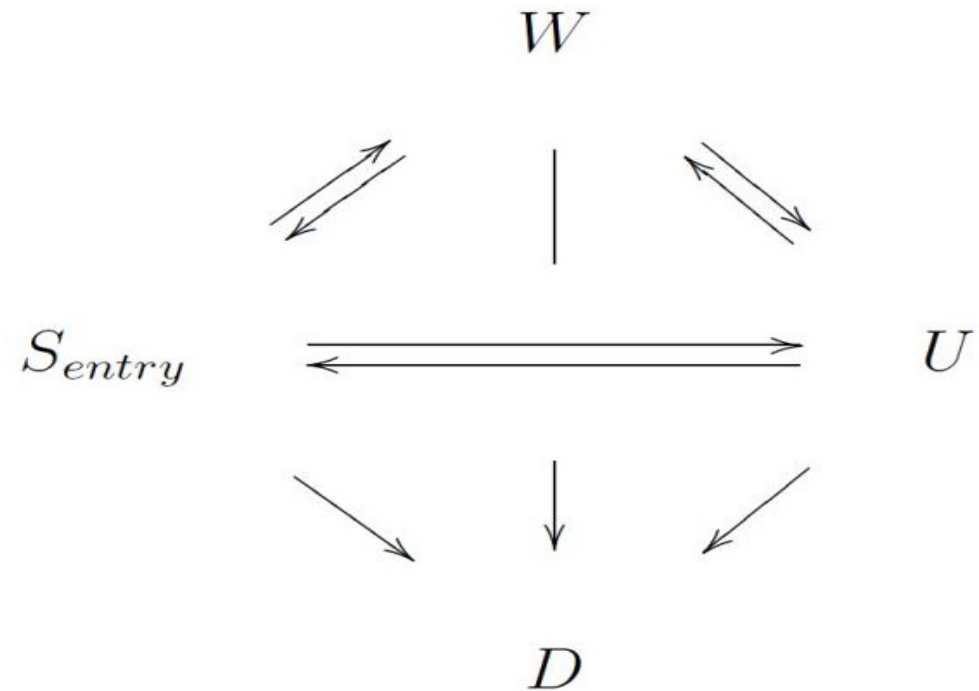
- Multi state models describe how individual moves between series of states in continuous time



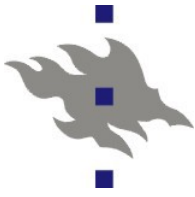


# Multi state modeling

- Multi state models describe how individual moves between series of states in continuous time



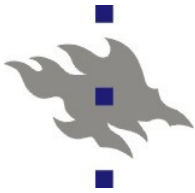
**Figure 1.** Model for transitions between the four states: **working (W)**, **sickness absence (S)**, **unemployment (U)** and **disability pension (D)**. The sickness absence state is labeled “entry”, to indicate that only sick-listed persons enter the study. (Pedersen J, Bjorner JB, Burr H, et al. *Transitions between sickness absence, work, unemployment, and disability in Denmark 2004-2008. Scand J Work Environ Health* 2012;38:516–26.)



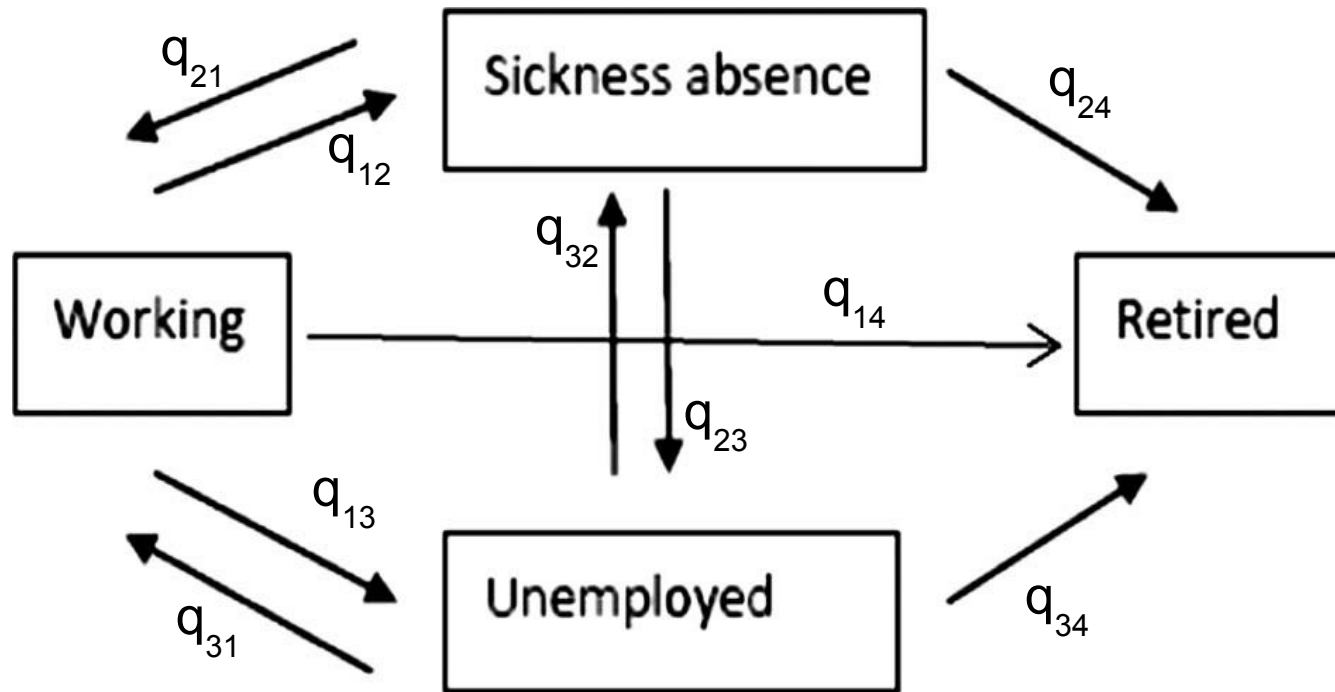
# Analysing multi-state data (1)

- One approach is that we are interested in transition pattern between states. We apply Markov model, where transition intensities between states are presented in matrix  $\mathbf{Q}$

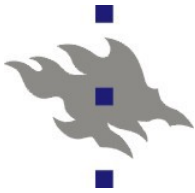
$$\mathbf{Q} = \begin{pmatrix} q_{11} & q_{12} & q_{13} \\ q_{21} & q_{22} & q_{23} \\ q_{31} & q_{32} & q_{33} \end{pmatrix}$$



# Transition example (1)



**Figure 1** Transition states between labour market outcomes in Denmark. Work, sickness absence and unemployment covers persons in the workforce while retirement independent of the reason (disability or age) is an irreversible state, where persons are considered to leave the workforce forever. (Carlsen K, Harling H, Pedersen J, et al. *The transition between work, sickness absence and pension in a cohort of Danish colorectal cancer survivors. BMJ Open* 2013;3. doi:10.1136/bmjopen-2012-002259)

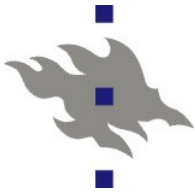


# Q with some constrains

1. Working
2. Sickness absence
3. Unemployed
4. Retired

$$Q = \begin{pmatrix} q_{11} & q_{12} & q_{13} & q_{14} \\ q_{21} & q_{22} & q_{23} & q_{24} \\ q_{31} & q_{32} & q_{33} & q_{34} \\ 0 & 0 & 0 & q_{44} \end{pmatrix}$$

Intensity matrix for Carlsen K, Harling H, Pedersen J (2013)



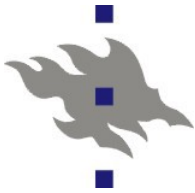
# Analysing multi-state data

- Using matrix **Q** we are able to calculate transition matrix P between states.
- $p_{ij}$  describes probability to be in state  $j$  after certain time when starting state is  $i$

$$Q = \begin{pmatrix} q_{11} & q_{12} & q_{13} & q_{14} \\ q_{21} & q_{22} & q_{23} & q_{24} \\ q_{31} & q_{32} & q_{33} & q_{34} \\ 0 & 0 & 0 & q_{44} \end{pmatrix} \quad P = \begin{pmatrix} p_{11} & p_{12} & p_{13} & p_{14} \\ p_{21} & p_{22} & p_{23} & p_{24} \\ p_{31} & p_{32} & p_{33} & p_{34} \\ p_{41} & p_{42} & p_{43} & p_{44} \end{pmatrix}$$

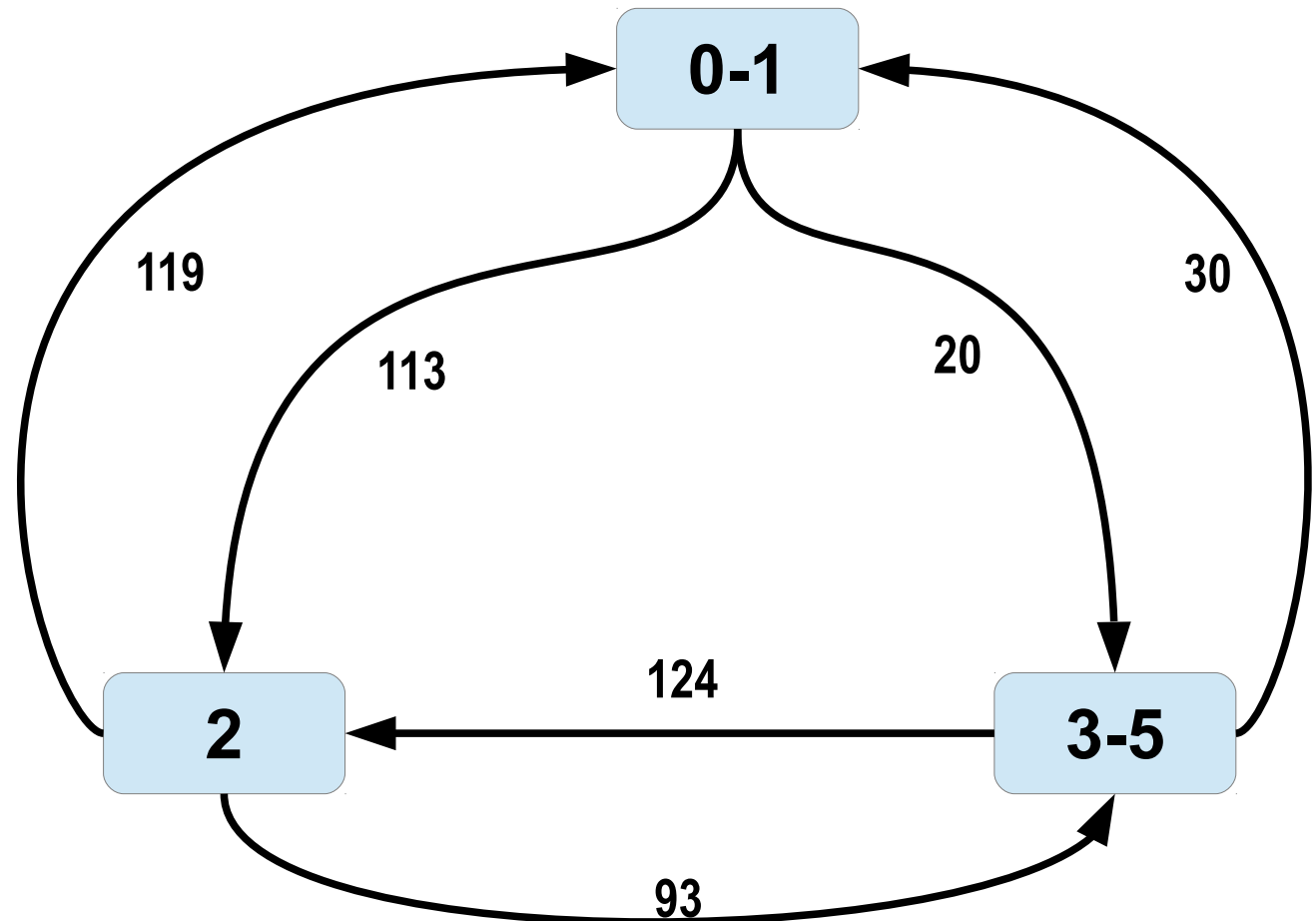
Intensity matrix for Carlsen K,  
Harling H, Pedersen J (2013)





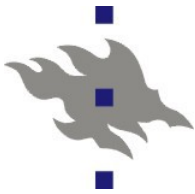
# States in nocturia data

	to		
from	0-1	2	3-5
1	333	113	20
2	119	272	93
3	30	124	432



## NOTE!

All transitions between states are possible. Here are number of transitions



# Example

- We use R package "msm" for analysis

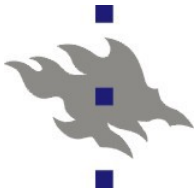
```
# Initial values for Q matrix
```

```
> twoway2.q
```

```
      0-1      2      3-5
0-1  0.000  0.166  0.166
2     0.166  0.000  0.166
3-5  0.166  0.166  0.000
```

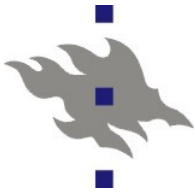
```
# Model without covariates
```

```
tmp.m1.msm <- msm(Noct.3.num ~ Week.num,
  subject = PATIENT, gen.inits = TRUE,
  qmatrix = twoway2.q,
  data = pla.data.1.V2,
  obstype = 1, analyticp = TRUE,
  opt.method = "optim",
  control = list(maxit = 1000,
    trace = 0, fnscale = 2000))
```



# Simple model results

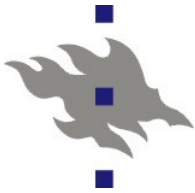
```
##
## Call:
## msm(formula = Noct.3.num ~ Week.num, subject = PATIENT, data =
pla.data.1.V2,      qmatrix = twoway2.q, gen.inits = TRUE, obstype
= 1, opt.method = "optim",      analyticp = TRUE, control =
list(maxit = 1000, trace = 0,      fnscale = 2000))
##
## Maximum likelihood estimates:
## Transition intensity matrix
##
##      0-1                2
## 0-1 -0.05529 (-0.0685,-0.04463) 0.05298 (0.042,0.06682)
## 2   0.05591 (0.04434,0.07049)   -0.09766 (-0.1153,-0.0827)
## 3-5 0.00321 (0.001195,0.008623) 0.04537 (0.04053,0.05078)
##      3-5
## 0-1 0.002316 (0.0005702,0.009405)
## 2   0.04176 (0.03352,0.05203)
## 3-5 -0.04858 (-0.05445,-0.04333)
##
## -2 * log-likelihood: 2658
```



# Simple model, intensity matrix

Intensity matrix ( $Q$ )

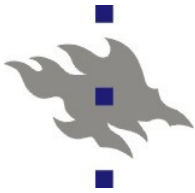
	0-1	2	3-5
0-1	-0.0553	0.0530	0.0023
2	0.0559	-0.0977	0.0418
3-5	0.0032	0.0454	-0.0486



# Adding covariates

- It is possible to add individual level covariates into model.
- We also might be interested in if transition intensities are stable or are they time-inhomogeneous (not shown here).

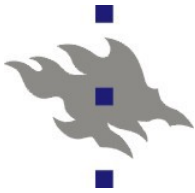
```
msm(formula = Noct.3.num ~ Week.num,  
     subject = PID, data = pla.data.2,  
     qmatrix = twoway2.q, gen.inits = TRUE,  
     obstype = 1, pci = c(27),  
     opt.method = "optim",  
     control = list(maxit = 1000, trace = 0,  
     fnscale = 2000))
```



# Model with covarites

```
# Add BMI as covariate
```

```
tmp.m2.msm <- msm(Noct.3.num ~ Week.num, subject = PATIENT,  
  gen.inits = TRUE,  
  qmatrix = twoway2.q, data = pla.data.1.V2[tmp.i., ],  
  obstype = 1, covariates = ~BMI..kg.m2.,  
  opt.method = "optim", control =  
  list(maxit = 1000, trace = 0, fnscale = 2000))
```

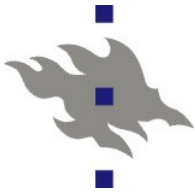


# Model comparison

- Now we have two models, viz. "tmp.m1.msm" and "tmp.m2.msm".
- We use likelihood ratio test to check if covariate (BMI) should be included.
- It turns out that BMI as covariate should be included

```
# Check model, adding BMI as covariate gives better  
# model  
lrtest.msm(tmp.m1.msm, tmp.m2.msm)
```

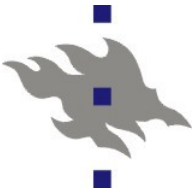
```
##           -2 log LR df           p  
## tmp.m2.msm      20.19  6 0.00256
```



# Interpretation of results

- In order to interpret results it is usually sensible to calculate estimates **transition matrices (TM)**.
- In this example we calculate TM for two covariate values: BMI=25 and BMI=30
- Transition matrix is calculated for time period of 24 week (6 months)





# Transition matrices estimates

- Predicted probability of transition (%) in 24 weeks.
- With two covariate values (BMI=25 and BMI=30)

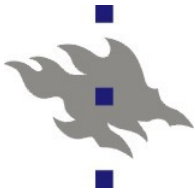
## BMI=25

	0-1		2		3-5
0-1	51 (45, 57)		33 (28, 37)		16 (13, 21)
2	37 (32, 42)		38 (33, 42)		26 (22, 31)
3-5	23 (20, 28)		34 (30, 37)		43 (37, 48)

## BMI=30

	0-1		2		3-5
0-1	45 (38, 51)		32 (28, 38)		23 (19, 28)
2	33 (28, 39)		35 (30, 39)		32 (27, 37)
3-5	22 (18, 26)		31 (27, 35)		47 (42, 52)

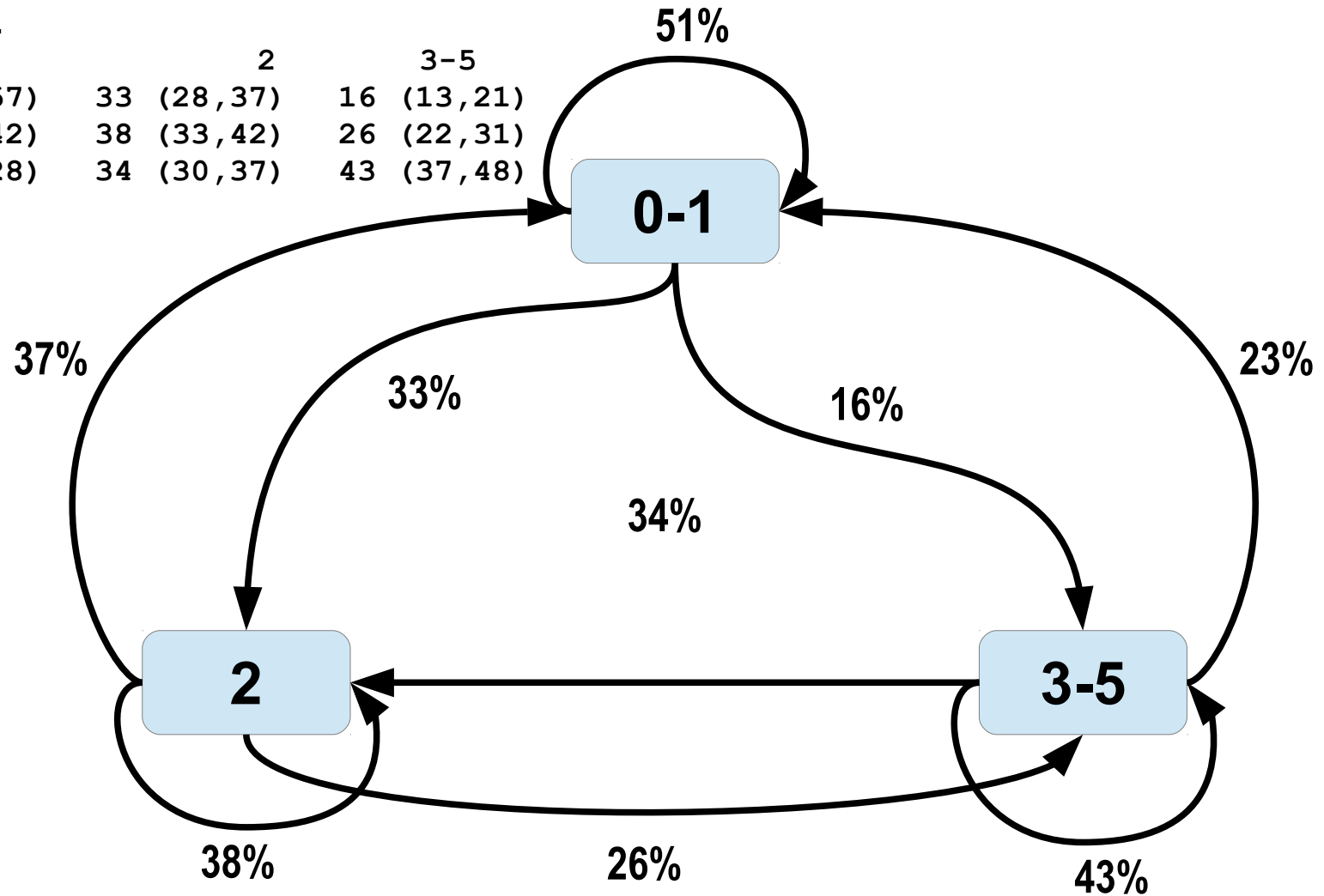
Transition prob. to state "3-5" is much higher for patients with higher BMI

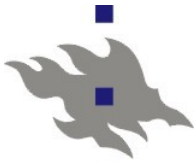


# 24 weeks transitions

**BMI=25**

	0-1	2	3-5
0-1	51 (45,57)	33 (28,37)	16 (13,21)
2	37 (32,42)	38 (33,42)	26 (22,31)
3-5	23 (20,28)	34 (30,37)	43 (37,48)

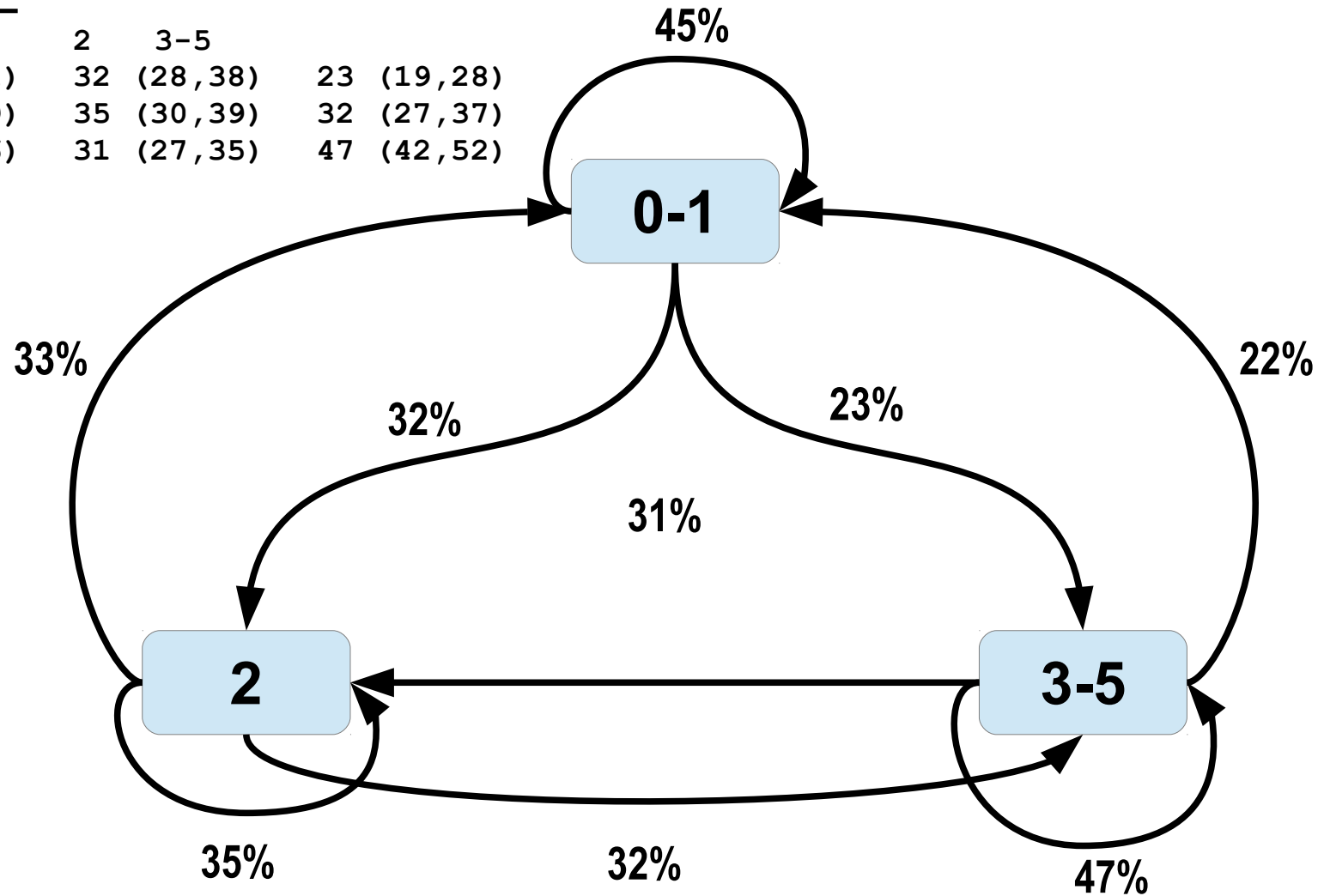


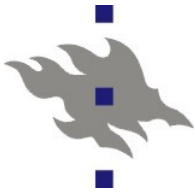


# 24 weeks transitions

**BMI=30**

	0-1	2	3-5			
0-1	45	(38, 51)	32	(28, 38)	23	(19, 28)
2	33	(28, 39)	35	(30, 39)	32	(27, 37)
3-5	22	(18, 26)	31	(27, 35)	47	(42, 52)

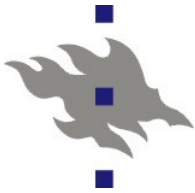




# Model with covariate(s)

- Effect of covariate(s) could be presented as hazard ratios (HR) for each transition
- Here HR presented for five units of BMI

```
print(hazard.msm(tmp.m2.msm, hazard.scale = 5))
## $BMI..kg.m2.
##           HR           L           U
## 0-1 - 2     1.1617  0.8475  1.593
## 0-1 - 3-5   1.8966  0.8879  4.051
## 2 - 0-1     1.0637  0.8199  1.380
## 2 - 3-5     1.2701  0.9502  1.698
## 3-5 - 0-1   1.0751  0.4494  2.572
## 3-5 - 2     0.9455  0.6939  1.288
```



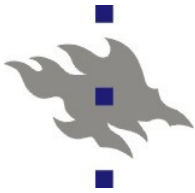
# Conclusion

**Question was:** Methodological challenges in research on consequences of sickness absence and disability pension?

**Answer:** Yes, there are such challenges. Two approaches,

- **Lexis** data with Poisson regression and
- **multi state** models,

might help researcher to have better grasp to data and the transitions of sickness absence and disability pension.



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